

# SNAPSHOTS

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# SNAPSHOT

— ALGEBRA I —

## Mathematical Process Standards

**A.1 Mathematical process standards.** The student uses mathematical processes to acquire and demonstrate mathematical understanding.

## Tools to Know

- A.1(A) apply mathematics to problems arising in everyday life, society, and the workplace  
 A.1(B) use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution  
 A.1(C) select tools, including real objects, manipulatives, paper and pencil, and technology as appropriate, and techniques, including mental math, estimation, and number sense as appropriate, to solve problems

## Linear Functions

Connected Knowledge and Skills A.4, A.5, A.12

**A.2 Linear functions, equations, and inequalities.** The student applies the mathematical process standards when using properties of linear functions to write and represent in multiple ways, with and without technology, linear equations, inequalities, and systems of equations.

**A.3 Linear functions, equations, and inequalities.** The student applies the mathematical process standards when using graphs of linear functions, key features, and related transformations to represent in multiple ways and solve, with and without technology, equations, inequalities, and systems of equations.

STAAR	Readiness Standards	Supporting Standards
19-20 items	<p>A.2(A) determine the domain and range of a linear function in mathematical problems; determine reasonable domain and range values for real-world situations, both continuous and discrete; and represent domain and range using inequalities</p> <p>A.2(C) write linear equations in two variables given a table of values, a graph, and a verbal description</p> <p>A.3(B) calculate the rate of change of a linear function represented tabularly, graphically, or algebraically in context of mathematical and real-world problems</p> <p>A.3(C) graph linear functions on the coordinate plane and identify key features, including x-intercept, y-intercept, zeros, and slope, in mathematical and real-world problems</p> <p>A.5(A) solve linear equations in one variable, including those for which the application of the distributive property is necessary and for which variables are included on both sides</p>	<p>A.2(B) write linear equations in two variables in various forms, including <math>y = mx + b</math>, <math>Ax + By = C</math>, and <math>y - y_1 = m(x - x_1)</math>, given one point and the slope and given two points</p> <p>A.2(D) write and solve equations involving direct variation</p> <p>A.2(E) write the equation of a line that contains a given point and is parallel to a given line</p> <p>A.2(F) write the equation of a line that contains a given point and is perpendicular to a given line</p> <p>A.2(G) write an equation of a line that is parallel or perpendicular to the x- or y-axis and determine whether the slope of the line is zero or undefined</p> <p>A.3(A) determine the slope of a line given a table of values, a graph, two points on the line, and an equation written in various forms, including <math>y = mx + b</math>, <math>Ax + By = C</math>, and <math>y - y_1 = m(x - x_1)</math></p> <p>A.3(E) determine the effects on the graph of the parent function <math>f(x) = x</math> when <math>f(x)</math> is replaced by <math>af(x)</math>, <math>f(x) + d</math>, <math>f(x - c)</math>, <math>f(bx)</math> for specific values of <math>a</math>, <math>b</math>, <math>c</math>, and <math>d</math></p> <p>A.4(A) calculate, using technology, the correlation coefficient between two quantitative variables and interpret this quantity as a measure of the strength of the linear association</p> <p>A.4(B) compare and contrast association and causation in real-world problems</p> <p>A.4(C) write, with and without technology, linear functions that provide a reasonable fit to data to estimate solutions and make predictions for real-world problems</p> <p>A.12(A) decide whether relations represented verbally, tabularly, graphically, and symbolically define a function</p> <p>A.12(B) evaluate functions, expressed in function notation, given one or more elements in their domains</p> <p>A.12(C) identify terms of arithmetic and geometric sequences when the sequences are given in function form using recursive processes</p> <p>A.12(D) write a formula for the <math>n^{\text{th}}</math> term of arithmetic and geometric sequences, given the value of several of their terms</p> <p>A.12(E) solve mathematic and scientific formulas, and other literal equations, for a specified variable</p>

## Systems of Equations and Inequalities

- A.2 Linear functions, equations, and inequalities.** The student applies the mathematical process standards when using properties of linear functions to write and represent in multiple ways, with and without technology, linear equations, inequalities, and systems of equations.
- A.3 Linear functions, equations, and inequalities.** The student applies the mathematical process standards when using graphs of linear functions, key features, and related transformations to represent in multiple ways and solve, with and without technology, equations, inequalities, and systems of equations.
- A.5 Linear functions, equations, and inequalities.** The student applies the mathematical process standards to solve, with and without technology, linear equations and evaluate the reasonableness of their solutions.

STAAR	Readiness Standards	Supporting Standards
8-9 items	<p>A.2(I) write systems of two linear equations given a table of values, a graph, and a verbal description</p> <p>A.3(D) graph the solution set of linear inequalities in two variables on the coordinate plane</p> <p>A.5(C) solve systems of two linear equations with two variables for mathematical and real-world problems</p>	<p>A.2(H) write linear inequalities in two variables given a table of values, a graph, and a verbal description</p> <p>A.3(F) graph systems of two linear equations in two variables on the coordinate plane and determine the solutions if they exist</p> <p>A.3(G) estimate graphically the solutions to systems of two linear equations with two variables in real-world problems</p> <p>A.3(H) graph the solution set of systems of two linear inequalities in two variables on the coordinate plane</p> <p>A.5(B) solve linear inequalities in one variable, including those for which the application of the distributive property is necessary and for which variables are included on both sides</p>

## Simplifying Expressions

- A.10 Number and algebraic methods.** The student applies the mathematical process standards and algebraic methods to rewrite in equivalent forms and perform operations on polynomial expressions.
- A.11 Number and algebraic methods.** The student applies the mathematical process standards and algebraic methods to rewrite algebraic expressions into equivalent forms.

8-9 items	<p>A.10(E) factor, if possible, trinomials with real factors in the form <math>ax^2 + bx + c</math>, including perfect square trinomials of degree two</p> <p>A.11(B) simplify numeric and algebraic expressions using the laws of exponents, including integral and rational exponents</p>	<p>A.10(A) add and subtract polynomials of degree one and degree two</p> <p>A.10(B) multiply polynomials of degree one and degree two</p> <p>A.10(C) determine the quotient of a polynomial of degree one and polynomial of degree two when divided by a polynomial of degree one and polynomial of degree two when the degree of the divisor does not exceed the degree of the dividend</p> <p>A.10(D) rewrite polynomial expressions of degree one and degree two in equivalent forms using the distributive property</p> <p>A.10(F) decide if a binomial can be written as the difference of two squares and, if possible, use the structure of a difference of two squares to rewrite the binomial</p> <p>A.11(A) simplify numerical radical expressions involving square roots</p>
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Quadratic Functions		Connected Knowledge and Skills A.12
<p><b>A.6 Quadratic functions and equations.</b> The student applies the mathematical process standards when using properties of quadratic functions to write and represent in multiple ways, with and without technology, quadratic equations.</p> <p><b>A.7 Quadratic functions and equations.</b> The student applies the mathematical process standards when using graphs of quadratic functions and their related transformations to represent in multiple ways and determine, with and without technology, the solutions to equations.</p> <p><b>A.8 Quadratic functions and equations.</b> The student applies the mathematical process standards to solve, with and without technology, quadratic equations and evaluate the reasonableness of their solutions. The student formulates statistical relationships and evaluates their reasonableness based on real-world data.</p>		
STAAR	Readiness Standards	Supporting Standards
11-12 items	<p>A.6(A) determine the domain and range of quadratic functions and represent the domain and range using inequalities</p> <p>A.7(A) graph quadratic functions on the coordinate plane and use the graph to identify key attributes, if possible, including x-intercept, y-intercept, zeros, maximum value, minimum values, vertex, and the equation of the axis of symmetry</p> <p>A.7(C) determine the effects on the graph of the parent function <math>f(x) = x^2</math> when <math>f(x)</math> is replaced by <math>af(x)</math>, <math>f(x) + d</math>, <math>f(x - c)</math>, <math>f(bx)</math> for specific values of <math>a</math>, <math>b</math>, <math>c</math>, and <math>d</math></p> <p>A.8(A) solve quadratic equations having real solutions by factoring, taking square roots, completing the square, and applying the quadratic formula</p>	<p>A.6(B) write equations of quadratic functions given the vertex and another point on the graph, write the equation in vertex form (<math>f(x) = a(x - h)^2 + k</math>), and rewrite the equation from vertex form to standard form (<math>f(x) = ax^2 + bx + c</math>)</p> <p>A.6(C) write quadratic functions when given real solutions and graphs of their related equations</p> <p>A.7(B) describe the relationship between the linear factors of quadratic expressions and the zeros of their associated quadratic functions</p> <p>A.8(B) write, using technology, quadratic functions that provide a reasonable fit to data to estimate solutions and make predictions for real-world problems</p> <p>A.12(A) decide whether relations represented verbally, tabularly, graphically, and symbolically define a function</p> <p>A.12(B) evaluate functions, expressed in function notation, given one or more elements in their domains</p>

Exponential Functions		Connected Knowledge and Skills A.12
<p><b>A.9 Exponential functions and equations.</b> The student applies the mathematical process standards when using properties of exponential functions and their related transformations to write, graph, and represent in multiple ways exponential equations and evaluate, with and without technology, the reasonableness of their solutions. The student formulates statistical relationships and evaluates their reasonableness based on real-world data.</p>		
6-7 items	<p>A.9(C) write exponential functions in the form <math>f(x) = ab^x</math> (where <math>b</math> is a rational number) to describe problems arising from mathematical and real-world situations, including growth and decay</p> <p>A.9(D) graph exponential functions that model growth and decay and identify key features, including y-intercept and asymptote, in mathematical and real-world problems</p>	<p>A.9(A) determine the domain and range of exponential functions of the form <math>f(x) = ab^x</math> and represent the domain and range using inequalities</p> <p>A.9(B) interpret the meaning of the values of <math>a</math> and <math>b</math> in exponential functions of the form <math>f(x) = ab^x</math> in real-world problems</p> <p>A.9(E) write, using technology, exponential functions that provide a reasonable fit to data and make predictions for real-world problems</p> <p>A.12(A) decide whether relations represented verbally, tabularly, graphically, and symbolically define a function</p> <p>A.12(C) identify terms of <b>arithmetic</b> and geometric sequences when the sequences are given in function form using recursive processes</p> <p>A.12(D) write a formula for the <math>n^{\text{th}}</math> term of <b>arithmetic</b> and geometric sequences, given the value of several of their terms</p>
54 items (5 Griddable)	32-35 questions from Readiness Standards	19-22 questions from Supporting Standards

## Mathematical Process Standards

**A.1 Mathematical process standards.** The student uses mathematical processes to acquire and demonstrate mathematical understanding.

## Ways to Show

- A.1(D) communicate mathematical ideas, reasoning, and their implications using multiple representations, including symbols, diagrams, graphs, and language as appropriate
- A.1(E) create and use representations to organize, record, and communicate mathematical ideas
- A.1(F) analyze mathematical relationships to connect and communicate mathematical ideas
- A.1(G) display, explain, and justify mathematical ideas and arguments using precise mathematical language in written or oral communication

NOTE: The classification of standards on this Snapshot represents the reviewed and synthesized input of a sample of Texas Math teachers. This Snapshot DOES NOT represent a publication of the Texas Education Agency. District curriculum may reflect other classifications.

# **SNAPSHOT**

— ALGEBRA II —

### Mathematical Process Standards

**2A.1 Mathematical process standards.** The student uses mathematical processes to acquire and demonstrate mathematical understanding.

#### Tools to Know

2A.1(A) apply mathematics to problems arising in everyday life, society, and the workplace

2A.1(B) use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution

2A.1(C) select tools, including real objects, manipulatives, paper and pencil, and technology as appropriate, and techniques, including mental math, estimation, and number sense as appropriate, to solve problems

### Absolute Value Functions

Connected Knowledge and Skills 2A.7

**2A.2 Attributes of functions and their inverses.** The student applies mathematical processes to understand that functions have distinct key attributes and understand the relationship between a function and its inverse.

**2A.6 Cubic, cube root, absolute value and rational functions, equations, and inequalities.** The student applies mathematical processes to understand that cubic, cube root, absolute value and rational functions, equations, and inequalities can be used to model situations, solve problems, and make predictions.

#### Readiness Standards

2A.2(A) graph the functions  $f(x)=\sqrt{x}$ ,  $f(x)=1/x$ ,  $f(x)=x^3$ ,  $f(x)=\sqrt[3]{x}$ ,  $f(x)=b^x$ ,  $f(x)=|x|$ , and  $f(x)=\log_b(x)$  where  $b$  is 2, 10, and  $e$  and, when applicable, analyze the key attributes such as domain, range, intercepts, symmetries, asymptotic behavior, and maximum and minimum given an interval

2A.6(E) solve absolute value linear equations

#### Supporting Standards

2A.6(C) analyze the effect on the graphs of  $f(x) = |x|$  when  $f(x)$  is replaced by  $af(x)$ ,  $f(bx)$ ,  $f(x-c)$ , and  $f(x) + d$  for specific positive and negative real values of  $a$ ,  $b$ ,  $c$ , and  $d$

2A.6(D) formulate absolute value linear equations

2A.6(F) solve absolute value linear inequalities

2A.7(I) write the domain and range of a function in interval notation, inequalities, and set notation

### Systems of Equations and Inequalities

**2A.3 Systems of equations and inequalities.** The student applies mathematical processes to formulate systems of equations and inequalities, use a variety of methods to solve, and analyze reasonableness of solutions.

2A.3(B) solve systems of three linear equations in three variables by using Gaussian elimination, technology with matrices, and substitution

2A.3(E) formulate systems of at least two linear inequalities in two variables

2A.3(F) solve systems of two or more linear inequalities in two variables

2A.3(G) determine possible solutions in the solution set of systems of two or more linear inequalities in two variables

## Quadratic and Square Root Functions

Connected Knowledge and Skills 2A.3, 2A.7

- 2A.2 Attributes of functions and their inverses.** The student applies mathematical processes to understand that functions have distinct key attributes and understand the relationship between a function and its inverse.
- 2A.4 Quadratic and square root functions, equations, and inequalities.** The student applies mathematical processes to understand that quadratic and square root functions, equations, and quadratic inequalities can be used to model situations, solve problems, and make predictions.
- 2A.8 Data.** The student applies mathematical processes to analyze data, select appropriate models, write corresponding functions, and make predictions.

Readiness Standards	Supporting Standards
<p>2A.2(A) graph the functions <math>f(x)=\sqrt{x}</math>, <math>f(x)=1/x</math>, <math>f(x)=x^3</math>, <math>f(x)=\sqrt[3]{x}</math>, <math>f(x)=b^x</math>, <math>f(x)= x </math>, and <math>f(x)=\log_b(x)</math> where <math>b</math> is 2, 10, and <math>e</math> and, when applicable, analyze the key attributes such as domain, range, intercepts, symmetries, asymptotic behavior, and maximum and minimum given an interval</p> <p>2A.2(C) describe and analyze the relationship between a function and its inverse (quadratic and square root, logarithmic and exponential), including the restriction(s) on domain, which will restrict its range</p> <p>2A.3(A) formulate systems of equations, including systems consisting of three linear equations in three variables and systems consisting of two equations, the first linear and the second quadratic</p> <p>2A.4(B) write the equation of a parabola using given attributes, including vertex, focus, directrix, axis of symmetry, and direction of opening</p> <p>2A.4(C) determine the effect on the graph of <math>f(x) = \sqrt{x}</math> when <math>f(x)</math> is replaced by <math>af(x)</math>, <math>f(x) + d</math>, <math>f(bx)</math>, and <math>f(x - c)</math> for specific positive and negative values of <math>a</math>, <math>b</math>, <math>c</math>, and <math>d</math></p> <p>2A.4(F) solve quadratic and square root equations</p> <p>2A.8(C) predict and make decisions and critical judgments from a given set of data using linear, quadratic, and exponential models</p>	<p>2A.2(B) graph and write the inverse of a function using notation such as <math>f^{-1}(x)</math></p> <p>2A.2(D) use the composition of two functions, including the necessary restrictions on the domain, to determine if the functions are inverses of each other</p> <p>2A.3(C) solve, algebraically, systems of two equations in two variables consisting of a linear equation and a quadratic equation</p> <p>2A.3(D) determine the reasonableness of solutions to systems of a linear equation and a quadratic equation in two variables</p> <p>2A.4(A) write the quadratic function given three specified points in the plane</p> <p>2A.4(D) transform a quadratic function <math>f(x) = ax^2 + bx + c</math> to the form <math>f(x) = a(x - h)^2 + k</math> to identify the different attributes of <math>f(x)</math></p> <p>2A.4(E) formulate quadratic and square root equations using technology given a table of data</p> <p>2A.4(G) identify extraneous solutions of square root equations</p> <p>2A.4(H) solve quadratic inequalities</p> <p>2A.7(A) add, subtract, and multiply complex numbers</p> <p>2A.7(I) write the domain and range of a function in interval notation, inequalities, and set notation</p> <p>2A.8(A) analyze data to select the appropriate model from among linear, quadratic, and exponential models</p> <p>2A.8(B) use regression methods available through technology to write a linear function, a quadratic function, and an exponential function from a given set of data</p>

## Cube Root, Cubic, and Other Polynomial Functions

Connected Knowledge and Skills 2A.6

- 2A.2 Attributes of functions and their inverses.** The student applies mathematical processes to understand that functions have distinct key attributes and understand the relationship between a function and its inverse.
- 2A.7 Number and algebraic methods.** The student applies mathematical processes to simplify and perform operations on expressions and to solve equations.

<p>2A.2(A) graph the functions <math>f(x)=\sqrt{x}</math>, <math>f(x)=1/x</math>, <math>f(x)=x^3</math>, <math>f(x)=\sqrt[3]{x}</math>, <math>f(x)=b^x</math>, <math>f(x)= x </math>, and <math>f(x)=\log_b(x)</math> where <math>b</math> is 2, 10, and <math>e</math> and, when applicable, analyze the key attributes such as domain, range, intercepts, symmetries, asymptotic behavior, and maximum and minimum given an interval</p> <p>2A.2(C) describe and analyze the relationship between a function and its inverse (quadratic and square root, logarithmic and exponential), including the restriction(s) on domain, which will restrict its range</p> <p>2A.7(E) determine linear and quadratic factors of a polynomial expression of degree three and of degree four, including factoring the sum and difference of two cubes and factoring by grouping</p> <p>2A.7(H) solve equations involving rational exponents</p>	<p>2A.2(B) graph and write the inverse of a function using notation such as <math>f^{-1}(x)</math></p> <p>2A.2(D) use the composition of two functions, including the necessary restrictions on the domain, to determine if the functions are inverses of each other</p> <p>2A.6(A) analyze the effect on the graphs of <math>f(x) = x^3</math> and <math>f(x) = \sqrt[3]{x}</math> when <math>f(x)</math> is replaced by <math>af(x)</math>, <math>f(bx)</math>, <math>f(x - c)</math>, and <math>f(x) + d</math> for specific positive and negative real values of <math>a</math>, <math>b</math>, <math>c</math>, and <math>d</math></p> <p>2A.6(B) solve cube root equations that have real roots</p> <p>2A.7(B) add, subtract, and multiply polynomials</p> <p>2A.7(C) determine the quotient of a polynomial of degree three and of degree four when divided by a polynomial of degree one and of degree two</p> <p>2A.7(D) determine the linear factors of a polynomial function of degree three and of degree four using algebraic methods</p> <p>2A.7(G) rewrite radical expressions that contain variables to equivalent forms</p>
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Exponential and Logarithmic Functions		Connected Knowledge and Skills 2A.7
<b>2A.2</b>	<b>Attributes of functions and their inverses.</b> The student applies mathematical processes to understand that functions have distinct key attributes and understand the relationship between a function and its inverse.	
<b>2A.5</b>	<b>Exponential and logarithmic functions and equations.</b> The student applies mathematical processes to understand that exponential and logarithmic functions can be used to model situations and solve problems.	
<b>2A.8</b>	<b>Data.</b> The student applies mathematical processes to analyze data, select appropriate models, write corresponding functions, and make predictions.	
Readiness Standards		Supporting Standards
2A.2(A)	graph the functions $f(x)=\sqrt{x}$ , $f(x)=1/x$ , $f(x)=x^3$ , $f(x)=\sqrt[3]{x}$ , $f(x)=b^x$ , $f(x)= x $ , and $f(x)=\log_b(x)$ where $b$ is 2, 10, and $e$ , and, when applicable, analyze the key attributes such as domain, range, intercepts, symmetries, asymptotic behavior, and maximum and minimum given an interval	2A.2(B) graph and write the inverse of a function using notation such as $f^{-1}(x)$ 2A.5(B) formulate exponential and logarithmic equations that model real-world situations, including exponential relationships written in recursive notation
2A.2(C)	describe and analyze the relationship between a function and its inverse (quadratic and square root, logarithmic and exponential), including the restriction(s) on domain, which will restrict its range	2A.5(C) rewrite exponential equations as their corresponding logarithmic equations and logarithmic equations as their corresponding exponential equations
2A.5(A)	determine the effects on the key attributes on the graphs of $f(x) = b^x$ and $f(x) = \log_b(x)$ where $b$ is 2, 10, and $e$ when $f(x)$ is replaced by $af(x)$ , $f(x) + d$ , and $f(x - c)$ for specific positive and negative real values of $a$ , $c$ , and $d$	2A.5(E) determine the reasonableness of a solution to a logarithmic equation 2A.7(I) write the domain and range of a function in interval notation, inequalities, and set notation
2A.5(D)	solve exponential equations of the form $y = ab^x$ where $a$ is a nonzero real number and $b$ is greater than zero and not equal to one and single logarithmic equations having real solutions	2A.8(A) analyze data to select the appropriate model from among linear, quadratic, and exponential models
2A.8(C)	predict and make decisions and critical judgments from a given set of data using linear, quadratic, and exponential models	2A.8(B) use regression methods available through technology to write a linear function, a quadratic function, and an exponential function from a given set of data

Rational Functions		Connected Knowledge and Skills 2A.2
<b>2A.6</b>	<b>Cubic, cube root, absolute value and rational functions, equations, and inequalities.</b> The student applies mathematical processes to understand that cubic, cube root, absolute value and rational functions, equations, and inequalities can be used to model situations, solve problems, and make predictions.	
<b>2A.7</b>	<b>Number and algebraic method.</b> The student applies mathematical processes to understand that exponential and logarithmic functions can be used to model situations and solve problems.	
2A.2(A)	graph the functions $f(x)=\sqrt{x}$ , $f(x)=1/x$ , $f(x)=x^3$ , $f(x)=\sqrt[3]{x}$ , $f(x)=b^x$ , $f(x)= x $ , and $f(x)=\log_b(x)$ where $b$ is 2, 10, and $e$ , and, when applicable, analyze the key attributes such as domain, range, intercepts, symmetries, asymptotic behavior, and maximum and minimum given an interval	2A.6(G) analyze the effect on the graphs of $f(x) = 1/x$ when $f(x)$ is replaced by $af(x)$ , $f(bx)$ , $f(x-c)$ , and $f(x) + d$ for specific positive and negative real values of $a$ , $b$ , $c$ , and $d$
2A.6(I)	solve rational equations that have real solutions	2A.6(H) formulate rational equations that model real-world situations
2A.6(L)	formulate and solve equations involving inverse variation	2A.6(J) determine the reasonableness of a solution to a rational equation
2A.7(F)	determine the sum, difference, product, and quotient of rational expressions with integral exponents of degree one and of degree two	2A.6(K) determine the asymptotic restrictions on the domain of a rational function and represent domain and range using interval notation, inequalities, and set notation
		2A.7(C) determine the quotient of a polynomial of degree three and of degree four when divided by a polynomial of degree one and of degree two

Mathematical Process Standards	
<b>2A.1</b>	<b>Mathematical process standards.</b> The student uses mathematical processes to acquire and demonstrate mathematical understanding.
Ways to Show	
2A.1(D)	communicate mathematical ideas, reasoning, and their implications using multiple representations, including symbols, diagrams, graphs, and language as appropriate
2A.1(E)	create and use representations to organize, record, and communicate mathematical ideas
2A.1(F)	analyze mathematical relationships to connect and communicate mathematical ideas
2A.1(G)	display, explain, and justify mathematical ideas and arguments using precise mathematical language in written or oral communication

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**SNAPSHOT**

— GEOMETRY —

## Mathematical Process Standards

**G.1 Mathematical process standards.** The student uses mathematical processes to acquire and demonstrate mathematical understanding.

## Tools to Know

- G.1(A) apply mathematics to problems arising in everyday life, society, and the workplace  
 G.1(B) use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution  
 G.1(C) select tools, including real objects, manipulatives, paper and pencil, and technology as appropriate, and techniques, including mental math, estimation, and number sense as appropriate, to solve problems

## Coordinate and Transformational Geometry

Connected Knowledge and Skills G.12

- G.2 Coordinate and transformational geometry.** The student uses the process skills to understand the connections between algebra and geometry and uses the one- and two-dimensional coordinate systems to verify geometric conjectures.  
**G.3 Coordinate and transformational geometry.** The student uses the process skills to generate and describe rigid transformations (translation, reflection, and rotation) and non-rigid transformations (dilations that preserve similarity and reductions and enlargements that do not preserve similarity).

## Readiness Standards

- G.2(B) derive and use the distance, slope, and midpoint formulas to verify geometric relationships, including congruence of segments and parallelism or perpendicularity of pairs of lines  
 G.2(C) determine an equation of a line parallel or perpendicular to a given line that passes through a given point  
 G.3(B) determine the image or pre-image of a given two-dimensional figure under a composition of rigid transformations, a composition of non-rigid transformations, and a composition of both, including dilations where the center can be any point in the plane

## Supporting Standards

- G.2(A) determine the coordinates of a point that is a given fractional distance less than one from one end of a line segment to the other in one- and two-dimensional coordinate systems, including finding the midpoint  
 G.3(A) describe and perform transformations of figures in a plane using coordinate notation  
 G.3(C) identify the sequence of transformations that will carry a given pre-image onto an image on and off the coordinate plane  
 G.3(D) identify and distinguish between reflectional and rotational symmetry in a plane figure  
 G.12(E) show that the equation of a circle with center at the origin and radius  $r$  is  $x^2 + y^2 = r^2$  and determine the equation for the graph of a circle with radius  $r$  and center  $(h, k)$ ,  $(x - h)^2 + (y - k)^2 = r^2$

## Logical Argument and Constructions

Connected Knowledge and Skills G.12

- G.4 Logical argument and constructions.** The student uses the process skills with deductive reasoning to understand geometric relationships.  
**G.5 Logical argument and constructions.** The student uses constructions to validate conjectures about geometric figures.  
**G.6 Proof and congruence.** The student uses the process skills with deductive reasoning to prove and apply theorems by using a variety of methods such as coordinate, transformational, and axiomatic and formats such as two-column, paragraph, and flow chart.

- G.4(C) verify that a conjecture is false using a counterexample  
 G.5(A) investigate patterns to make conjectures about geometric relationships, including angles formed by parallel lines cut by a transversal, criteria required for triangle congruence, special segments of triangles, diagonals of quadrilaterals, interior and exterior angles of polygons, and special segments and angles of circles choosing from a variety of tools  
 G.6(A) verify theorems about angles formed by the intersection of lines and line segments, including vertical angles, and angles formed by parallel lines cut by a transversal and prove equidistance between the endpoints of a segment and points on its perpendicular bisector and apply these relationships to solve problems

- G.4(A) distinguish between undefined terms, definitions, postulates, conjectures, and theorems  
 G.4(B) identify and determine the validity of the converse, inverse, and contrapositive of a conditional statement and recognize the connection between a biconditional statement and a true conditional statement with a true converse  
 G.4(D) compare geometric relationships between Euclidean and spherical geometries, including parallel lines and the sum of the angles in a triangle  
 G.5(B) construct congruent segments, congruent angles, a segment bisector, an angle bisector, perpendicular lines, the perpendicular bisector of a line segment, and a line parallel to a given line through a point not on a line using a compass and a straightedge  
 G.5(C) use the constructions of congruent segments, congruent angles, angle bisectors, and perpendicular bisectors to make conjectures about geometric relationships  
 G.5(D) verify the Triangle Inequality theorem using constructions and apply the theorem to solve problems  
 G.6(E) prove a quadrilateral is a parallelogram, rectangle, square, or rhombus using opposite sides, opposite angles, or diagonals and apply these relationships to solve problems  
 G.12(A) apply theorems about circles, including relationships among angles, radii, chords, tangents, and secants, to solve non-contextual problems

## Triangles and Trigonometry

Connected Knowledge and Skills G.5

- G.6 Proof and congruence.** The student uses the process skills with deductive reasoning to prove and apply theorems by using a variety of methods such as coordinate, transformational, and axiomatic and formats such as two-column, paragraph, and flow chart.
- G.7 Similarity, proof, and trigonometry.** The student uses the process skills in applying similarity to solve problems.
- G.8 Similarity, proof, and trigonometry.** The student uses the process skills with deductive reasoning to prove and apply theorems by using a variety of methods such as coordinate, transformational, and axiomatic and formats such as two-column, paragraph, and flow chart.
- G.9 Similarity, proof, and trigonometry.** The student uses the process skills to understand and apply relationships in right triangles.

Readiness Standards	Supporting Standards
<p>G.5(A) investigate patterns to make conjectures about geometric relationships, including angles formed by parallel lines cut by a transversal, criteria required for triangle congruence, special segments of triangles, diagonals of quadrilaterals, interior and exterior angles of polygons, and special segments and angles of circles choosing from a variety of tools</p> <p>G.6(B) prove two triangles are congruent by applying the Side-Angle-Side, Angle-Side-Angle, Side-Side-Side, Angle-Angle-Side, and Hypotenuse-Leg congruence conditions</p> <p>G.7(B) apply the Angle-Angle criterion to verify similar triangles and apply the proportionality of the corresponding sides to solve problems</p> <p>G.9(A) determine the lengths of sides and measures of angles in a right triangle by applying the trigonometric ratios sine, cosine, and tangent to solve problems</p> <p>G.9(B) apply the relationships in special right triangles <math>30^\circ</math>-<math>60^\circ</math>-<math>90^\circ</math> and <math>45^\circ</math>-<math>45^\circ</math>-<math>90^\circ</math> and the Pythagorean theorem, including Pythagorean triples, to solve problems</p>	<p>G.6(C) apply the definition of congruence, in terms of rigid transformations, to identify congruent figures and their corresponding sides and angles</p> <p>G.6(D) verify theorems about the relationships in triangles, including proof of the Pythagorean Theorem, the sum of interior angles, base angles of isosceles triangles, midsegments, and medians, and apply these relationships to solve problems</p> <p>G.7(A) apply the definition of similarity in terms of a dilation to identify similar figures and their proportional sides and the congruent corresponding angles</p> <p>G.8(A) prove theorems about similar triangles, including the Triangle Proportionality theorem, and apply these theorems to solve problems</p> <p>G.8(B) identify and apply the relationships that exist when an altitude is drawn to the hypotenuse of a right triangle, including the geometric mean, to solve problems</p>

## Measurement of 2D and 3D Figures

- G.10 Two-dimensional and three-dimensional figures.** The student uses the process skills to recognize characteristics and dimensional changes of two- and three-dimensional figures.
- G.11 Two-dimensional and three-dimensional figures.** The student uses the process skills in the application of formulas to determine measures of two- and three-dimensional figures.
- G.12 Circles.** The student uses the process skills to understand geometric relationships and apply theorems and equations about circles.

<p>G.10(B) determine and describe how changes in the linear dimensions of a shape affect its perimeter, area, surface area, or volume, including proportional and non-proportional dimensional change</p> <p>G.11(B) determine the area of composite two-dimensional figures comprised of a combination of triangles, parallelograms, trapezoids, kites, regular polygons, or sectors of circles to solve problems using appropriate units of measure</p> <p>G.11(C) apply the formulas for the total and lateral surface area of three-dimensional figures, including prisms, pyramids, cones, cylinders, spheres, and composite figures, to solve problems using appropriate units of measure</p> <p>G.11(D) apply the formulas for the volume of three-dimensional figures, including prisms, pyramids, cones, cylinders, spheres, and composite figures, to solve problems using appropriate units of measure</p>	<p>G.10(A) identify the shapes of two-dimensional cross-sections of prisms, pyramids, cylinders, cones, and spheres and identify three-dimensional objects generated by rotations of two-dimensional shapes</p> <p>G.11(A) apply the formula for the area of regular polygons to solve problems using appropriate units of measure</p> <p>G.12(B) apply the proportional relationship between the measure of an arc length of a circle and the circumference of the circle to solve problems</p> <p>G.12(C) apply the proportional relationship between the measure of the area of a sector of a circle and the area of the circle to solve problems</p> <p>G.12(D) describe radian measure of an angle as the ratio of the length of an arc intercepted by a central angle and the radius of the circle</p>
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## Probability

- G.13 Probability.** The student uses the process skills to understand probability in real-world situations and how to apply independence and dependence of events.

<p>G.13(C) identify whether two events are independent and compute the probability of the two events occurring together with or without replacement</p>	<p>G.13(A) develop strategies to use permutations and combinations to solve contextual problems</p> <p>G.13(B) determine probabilities based on area to solve contextual problems</p> <p>G.13(D) apply conditional probability in contextual problems</p> <p>G.13(E) apply independence in contextual problems</p>
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**Mathematical Process Standards**

**G.1 Mathematical process standards.** The student uses mathematical processes to acquire and demonstrate mathematical understanding.

**Ways to Show**

- G.1(D) communicate mathematical ideas, reasoning, and their implications using multiple representations, including symbols, diagrams, graphs, and language as appropriate
- G.1(E) create and use representations to organize, record, and communicate mathematical ideas
- G.1(F) analyze mathematical relationships to connect and communicate mathematical ideas
- G.1(G) display, explain, and justify mathematical ideas and arguments using precise mathematical language in written or oral communication

NOTE: The classification of standards on this Snapshot represents the reviewed and synthesized input of a sample of Texas Math teachers. This Snapshot DOES NOT represent a publication of the Texas Education Agency. District curriculum may reflect other classifications.